New Digital Signal Processing Algorithms for Frequency Deviation Measurement

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Abstract: This paper introduces two digital signal processing algorithms for frequency deviation measurement. The algorithms are derived using a new signal processing scheme based on quadratic forms of signal samples. These algorithms provide high measurement accuracy over a wide range of frequency changes. One is designed for measurements of small deviations of the nominal frequency whereas the other one measures offnominal frequency deviations. Performance of the algorithms is evaluated using computer simulation tests.

Keywords: Frequency measurements, Digital algorithms, Signal processing, Quadratic forms.

INTRODUCTION

This paper is concerned with two issues: the small frequency deviation measurements and the off-nominal frequency deviation measurements. Frequency information is one of the most important parameters for system monitoring and control. Load shedding, load restoration, generator protection from overspeeding and detection of the generation-load out-of-step conditions may in general be based on the small frequency deviation measurements. For generators, the over-excitation detection and the voltage and current estimates during start-up and shut-down procedures may be based on the off-nominal frequency deviation measurements.

Previous work in this field has resulted in a variety of algorithms for the small frequency deviation measurements. Some of these algorithms use known signal processing techniques such as Discrete Fourier Transform, Least Error Squares, and Kalman Filtering [1-5], while others use a heuristic approach [6, 7]. Most of them use the sinusoidal model for the signal. Their efficiency (accuracy) is influenced by one or more of the following factors: superimposed noise, non-linear static characteristic, and slow response. In general, increased accuracy and robustness require greater complexity. The query for more accurate, computationally simple and robust algorithms continues.

The off-nominal frequency deviation measurement algorithms were proposed in two references [8, 9]. Both use the results of a small frequency deviation algorithm and calculate the required correction. One is using the phase-locked loop and the other one is using a look-up table for correcting the estimate. Both of these methods are relatively complex and slow.

This paper presents two algorithms for measurement of frequency deviations. The first algorithm is the result of an attempt to overcome the deficiences in the small frequency deviation algorithms stated above. The approach was to look into existing frequency measurement algorithms for a common expression that could be utilized for the development of an accurate estimate of the frequency deviation [10]. The new process of determining the coefficients of this general form has resulted in a simple and accurate algorithm.

The second algorithm was designed to capture a wide range of the off-nominal frequency deviations by adapting (extending) the frequency deviation algorithm developed by the authors in an earlier reference [10]. Only three more multiplications were introduced to achieve the improved accuracy. The algorithm remains extremely simple, fast and accurate. No table-looking and no iterations are necessary to calculate the correction.

Extensive testing was performed with both algorithms. Static and dynamic tests show high accuracy and fast response. Algorithm robustness was tested using additive noise tests and Electromagnetic Transient Program (EMTP) network simulation tests. Both algorithms performed well by not amplifying the noise and converging fast for the EMTP generated signal transients.

The general expression used to derive both algorithms was recognized earlier by the authors as being suitable for accurate measurements of a number of power system quantities [11-15]. This leads the authors to a conclusion that a custom designed signal processing chip may be developed to implement the generalized algorithm form. Selection of the appropriate coefficients may enable use of the same chip for various applications such as frequency deviation, line parameter, and power measurements.

First part of the paper gives theoretical background and the frequency algorithm design procedure. Second part outlines derivation of the new algorithm for measurements of the small frequency deviations. Third part presents a new, very accurate and extremely simple algorithm for off-nominal frequency deviation measurements. Fourth part provides results of the extensive testing performed using both algorithms.

NEW DSP APPROACH

This section presents theoretical background and design procedure of a Digital Signal Processing (DSP) approach used to derive new algorithms.

It starts by introducing a general algorithm expression. This expression is recognized to be a common form for most of the previously introduced non-recursive frequency deviation measurement algorithms. The general algorithm expression is a quotient of quadratic forms (QQF) of signal samples. This expression is made constant in time and real for all frequency deviations of a sinusoidal signal. This is achieved by imposing constraints on the coefficients of the quadratic forms. Finally, the Taylor expansions of the quadratic forms give a quotient of two frequency deviation polynomials whose coefficients can be chosen so that the quotient becomes equal to the value of the signal frequency deviation.

The second subsection gives the steps of a formal procedure for the design of algorithms for frequency deviation measurements. This procedure shows a way of deriving the quadratic forms' coefficients satisfying the performance requirements and the constraints derived in the first subsection.

Theoretical Background

The following quotient of quadratic forms of signal samples is recognized to be a general form for frequency deviation measurement algorithms [10]:

$$\Delta \hat{f} = \frac{\sum_{k=0}^{N-1} \sum_{m=0}^{N-1} \overline{a}_{km} x_{n-k} x_{n-m}}{\sum_{k=0}^{N-1} \sum_{m=0}^{N-1} b_{km} x_{n-k} x_{n-m}}$$

$$= \frac{KF\overline{A}}{KFB} \tag{1}$$

KF are the quadratic forms, \overline{a}_{km} and b_{km} form matrices $\overline{\mathbf{A}}$ and \mathbf{B} associated with quadratic forms. Their definition is given in APPENDIX A.

Let us assume the following input signal representation:

$$x(t) = X\cos(\omega t + \phi) \tag{2}$$

$$x_n = X \cos(\omega n \Delta t + \phi)$$

= $X \cos(nd + \phi)$ (3)

Electrical angle deviation Δd is proportional to the deviation of frequency since $\Delta d = \Delta \omega \cdot \Delta t = 2\pi \Delta f \cdot \Delta t$.

For simplicity, we shall use the electrical angle deviation estimate which is of the same form as the frequency deviation estimate given in the equation (1):

$$\triangle \hat{d} = \frac{\sum_{k=0}^{N-1} \sum_{m=0}^{N-1} a_{km} x_{n-k} x_{n-m}}{\sum_{k=0}^{N-1} \sum_{m=0}^{N-1} b_{km} x_{n-k} x_{n-m}}$$

$$= \frac{KFA}{KFB}$$
(4)

where $a_{km} = \overline{a}_{km}/(2\pi \Delta t)$.

Conditions for expression (4) to be constant and to give the value of the signal frequency deviation are derived as follows.

In the case of a sinusoidal waveform, given by equation (3), the value of a quadratic form is:

$$KF(n) = \sum_{k=0}^{N-1} \sum_{m=0}^{N-1} h_{km} X^2 \cos[(n-k)d + \phi] \cos[(n-m)d + \phi]$$

$$= \frac{X^2}{2} \sum_{k=0}^{N-1} \sum_{m=0}^{N-1} h_{km} \cos[(m-k)d]$$

$$+ \frac{X^2}{2} \sum_{k=0}^{N-1} \sum_{m=0}^{N-1} h_{km} \cos[(2n - (k+m))d + 2\phi]$$

$$= KF^c + KF^v(n)$$
(5)

Equation (5) shows that the value of the quadratic form, in the case of a sinusoidal signal, consists of a constant KF^c and an oscillating $KF^v(n)$ component.

The constant part KF^{c} , can be expressed in the following way [11]:

$$KF^{c} = \frac{X^{2}}{2} Re\{\mathbf{K}^{c}(e^{-jd})\}$$
 (6)

where:

$$\mathbf{K}^{c}(w) = \sum_{r=-N+1}^{N-1} h_{r}^{c} w^{r}$$

$$h_{r}^{c} = \sum_{k} \sum_{m} h_{k-m=r} h_{km}$$

$$w = e^{-jd}$$

Also, the variable part $KF^{v}(n)$, can be expressed as follows [11]:

$$KF^{v}(n) = \frac{X^{2}}{2} |\mathbf{K}^{v}(e^{-jd})| \cos\{arg[\mathbf{K}^{v}(e^{-jd})] + 2nd + 2\phi\}$$
 (7)

where:

$$\mathbf{K}^{v}(w) = \sum_{r=0}^{2N-2} h_{r}^{v} w^{r}$$

$$h_{r}^{v} = \sum_{k} \sum_{m} h_{k+m=r} h_{km}$$

$$w = e^{-jd}$$
(8)

Since for a steady state sinusoidal signal frequency deviation is constant, the oscillating component KF^{ν} should be identical to zero for all frequency deviations and for all n. It can easily be seen from the equation (8) that $KF^{\nu}(n)$ is identical to zero when the following conditions are satisfied:

$$h_r^v = 0$$
 (9)
 $r = 0, \dots, 2N - 2$

From the equation (9) one can see that these conditions are equivalent to saying that the sums of the elements h_{km} on the anti-diagonal and all the sub-anti-diagonals of the quadratic form matrix \mathbf{H} are equal to zero.

For the constant component KF^c to be real for all frequencies, it is sufficient for the quadratic form matrix to be symmetrical. For a symmetric matrix, the following holds:

$$\mathbf{K}^{c}(w) = h_{0}^{c} + 2 \sum_{\tau=0}^{N-1} h_{\tau}^{c} Re\{w^{\tau}\} = Re\{\mathbf{K}^{c}(w)\}$$
 (10)

where $w = e^{-j\alpha}$

Equations (9) and (10) produce a constant and real value for the quadratic form of equation (5) as follows:

$$KF(n) = h_0^c + 2 \sum_{r=0}^{N-1} h_r^c Re\{w^r\}$$
$$= \sum_{r=0}^{N-1} h_r \cos(rd)$$
(11)

Therefore, the QQF for frequency deviation measurements, given by equation (1), may now be expressed as follows:

where:

$$\triangle \hat{d} = \frac{\sum_{r=0}^{N-1} a_r \cos(rd)}{\sum_{r=0}^{N-1} b_r \cos(rd)}$$

$$= \frac{\mathbf{A}(d)}{\mathbf{B}(d)}$$

$$a_0 = \sum_k \sum_{m} a_{km}$$

$$b_0 = \sum_k \sum_{m} b_{km}$$

$$a_r = \sum_k \sum_{m} a_{km}$$

$$b_r = \sum_k \sum_{m} a_{km}$$

$$b_r = \sum_k \sum_{m} a_{km}$$

$$b_k = \sum_k \sum_{m} a_{km}$$

This form is constant and real for all deviations of the electrical angle. In order to obtain estimates of the electrical angle, functions **A** and **B** are expressed in the forms of their Taylor expansions. As a result, the following general expression for frequency deviation estimate is obtained:

$$\Delta \hat{d} = \frac{\mathbf{A}(d_0) + \mathbf{A}'(d_0)\Delta d + \mathbf{A}''(d_0)\frac{(\Delta d)^2}{2} + \cdots}{\mathbf{B}(d_0) + \mathbf{B}'(d_0)\Delta d + \mathbf{B}''(d_0)\frac{(\Delta d)^2}{2} + \cdots}$$
(13)

Equation (13) is the generic algorithm expression used in the next section to derive different algorithms.

Algorithm Design Procedure

The algorithm design procedure is related to the appropriate selection of coefficients in the generic algorithm expression given by equation (13). The algorithm is designed according to the application constraints. The following steps allow for the design of the algorithms for frequency deviation measurements.

- The following algorithm parameters are chosen: data window, number of signal samples, sampling frequency, measurement range, and degree of desired accuracy.
- The size of the quadratic forms' matrices is chosen using first three parameters.
- Last two algorithm parameters are used for selecting the order of the polynomials in the equation (13). Having selected the polynomial order, necessary constraints need to be imposed on the remaining coefficients. Incidentally, the most general set of conditions for the equation (13) to give the signal frequency deviation estimate can be determined.
- Two sparse symmetric quadratic forms' matrices are formed. The nonzero elements of these matrices are then selected to satisfy equation (9). Also, in order to satisfy the conditions derived in the third step, the total number of nonzero elements needs to be greater or equal to the number of these conditions.
- A frequency deviation algorithm is derived by solving the equations obtained in the third step for the unknown elements of the matrices formed in the fourth step.

 Last, noise sensitivity and the accuracy requirements are checked. If they are not satisfied one goes back to the fourth step to change the matrix elements. If necessary, one may also go back to the third step to select a different order for the polynomials.

SMALL FREQUENCY DEVIATION MEASUREMENT ALGORITHM

The described algorithm design procedure is implemented as follows.

If one chooses a data window length of three quarters of the nominal period, and a sampling rate of sixteen samples per cycle, then the nominal electric angle for this case is equal to $d_0 = \frac{\pi}{8}$.

To achieve high accuracy four terms of the Taylor expansions are used here. In this case, for equation (13) to give the signal frequency deviation, the most general set of conditions set upon the remaining polynomial coefficients is as follows:

$$\mathbf{A}(d_0) = 0
\mathbf{B}'''(d_0) = 0
\mathbf{A}'(d_0) = \mathbf{B}(d_0)
\frac{\mathbf{A}''(d_0)}{2} = \mathbf{B}'(d_0)
\frac{\mathbf{A}'''(d_0)}{3} = \mathbf{B}''(d_0)$$
(14)

In this case, the frequency deviation estimate given by equation (13) approximates the signal frequency deviation as follows:

$$\triangle \hat{d} \approx \triangle d \tag{15}$$

The goal is to determine the quadratic forms' coefficients. Accordingly, the fourth step of the frequency deviation measurement algorithm design procedure requires forming two sparse symmetric matrices whose sums of elements on the anti-diagonal and all the sub-anti-diagonals are equal to zero (follows from equation (9)). Another requirement is that these matrices have a greater (or equal) number of nonzero elements than the number of algorithm coefficients' constraints derived in the third step of the procedure.

Matrices of the following form are used:

Matrix B is a symmetric 13 by 13 matrix that can be reduced to an 8 by 8 matrix because the remaining elements are zero. Both matrices satisfy the above requirements. They have in total seven nonzero elements against the five algorithm coefficients' constraints given by equation (14). Two of these elements are assumed in a way that simplifies the calculation of other elements and enables getting small enough numbers for the other elements.

For matrices of this form, and for c=0.05 and d=0.01, coefficient constraints, expressed by equations (14), give as a result the following values for the coefficients of quadratic forms: $a=-1.044303503155235,\ b=0.52823862829380,\ e=0.78543321540189,\ f=-1.05813678372674$ and g=-0.03443924221845.

The estimate of the electrical angle deviation, given by equation (4), now becomes:

$$\Delta \hat{d} = \frac{x_n \cdot w_0 - x_{n-1} \cdot w_1}{x_n \cdot z_0 - x_{n-1} \cdot z_1} \tag{16}$$

where:

$$\begin{array}{rcl} w_0 & = & a \cdot x_{n-2} + b \cdot x_{n-3} + c \cdot x_{n-7} + d \cdot x_{n-12} \\ w_1 & = & a \cdot x_{n-1} + b \cdot x_{n-2} + c \cdot x_{n-6} + d \cdot x_{n-11} \\ z_0 & = & e \cdot x_{n-2} + f \cdot x_{n-3} + g \cdot x_{n-7} \\ z_1 & = & e \cdot x_{n-1} + f \cdot x_{n-2} + g \cdot x_{n-6}. \end{array}$$

Results presented in the algorithm testing section indicate high accuracy and low noise sensitivity of the obtained algorithm.

OFF-NOMINAL FREQUENCY MEASUREMENT ALGORITHM

Due to their simplicity, algorithms for small frequency deviation measurement do not calculate the off-nominal frequency deviation of the sinusoidal signal very accurately. As shown in reference [9], one can calculate the measurement error in an off-line mode. This error estimate can be used to improve the frequency deviation estimate.

The goal of this paper is to introduce an efficient and simple measurement algorithm for off-nominal frequency deviations. The Taylor expansion of the estimate error function is used to derive this new algorithm.

To design an algorithm that uses a data window which is equal to one half of the nominal period and a sampling rate of eight samples per cycle, one can proceed as follows. In this case the nominal electric angle is equal to $d_0 = \frac{\pi}{4}$.

Let us assume low influence of the Taylor expansion terms in equation (13) that are higher than the third order. To get an accurate estimate of the electric angle deviation, the following constraints for the coefficients of the frequency deviation polynomials are imposed.

$$\mathbf{A}(d_0) = 0
\mathbf{B}''(d_0) = 0
\frac{\mathbf{A}''(d_0)}{2} = \mathbf{B}'(d_0)
\mathbf{A}'(d_0) = \mathbf{B}(d_0)$$
(17)

In order to simplify the selection of the quadratic forms' coefficients, some of the coefficients are assumed to be zero. For the reasons given earlier, quadratic forms' matrices are

chosen to be symmetrical and to have the sums of the elements on the antidiagonal and all sub-antidiagonals equal to zero.

Hence, the matrices have this form:

$$\mathbf{A} = \begin{bmatrix} 0 & 0 & a & b & c \\ 0 & -2a & -b & 0 & 0 \\ a & -b & -2c & 0 & 0 \\ b & 0 & 0 & 0 & 0 \\ c & 0 & 0 & 0 & 0 \end{bmatrix}$$
$$\mathbf{B} = \begin{bmatrix} 0 & 0 & g & f & h \\ 0 & -2g & -f & 0 & 0 \\ g & -f & -2h & 0 & 0 \\ f & 0 & 0 & 0 & 0 \\ h & 0 & 0 & 0 & 0 \end{bmatrix}$$

Furthermore, for f=0 and g=1, equations (17) give as a result the following values for the coefficients of quadratic forms: a=0.5, b=0, c=-0.25 and h=0.

After the selection of the quadratic forms' coefficients, equation (4) gives as a result the following algorithm for determining the electrical angle deviation estimate:

$$\Delta \hat{d} = 0.5 \cdot \left[1 - 0.5 \cdot \frac{x_n \cdot x_{n-4} - x_{n-2}^2}{x_n \cdot x_{n-2} - x_{n-1}^2} \right]$$
 (18)

For a sinusoidal signal $x = X \cos(nd + \phi)$, equation (12) gives:

$$\Delta \hat{d} = \frac{-0.5 + \cos(2d) - 0.5\cos(4d)}{2 \cdot [\cos(2d) - 1]}$$
$$= \frac{\sin(2\Delta d)}{2}, \quad d = d_0 + \Delta d$$
(19)

This equation is much simpler than the one given in reference [9]. Following the approach given in reference [9], a more accurate estimate for off-nominal frequency deviation can be obtained. This is achieved by using an arcsin look-up table which helps to solve the following equation:

$$\triangle d = \frac{\arcsin(2 \cdot \triangle \hat{d})}{2} \tag{20}$$

A different approach that obviates the need for a look-up table and gives a more simple solution is described here.

Five terms of the arcsine Taylor expansion series provide the following corrected electrical angle estimate:

$$\Delta \hat{d} = 0.5 \cdot \left[1 - 0.5 \cdot \frac{x_n \cdot x_{n-4} - x_{n-2}^2}{x_n \cdot x_{n-2} - x_{n-1}^2} \right]$$

$$\Delta \hat{d}_1 = \Delta \hat{d} \cdot \Delta \hat{d}$$

$$\Delta \hat{d}_2 = \Delta \hat{d}_1 \cdot \Delta \hat{d}_1$$

$$\Delta \hat{d}_{corr} = \Delta \hat{d} \cdot \left(1 + \frac{\Delta \hat{d}_1}{6} + 3 \cdot \frac{\Delta \hat{d}_2}{40} \right)$$
(21)

Only three new estimate multiplications are introduced. In this way the algorithm remains extremely simple and easy to implement.

Test results given below show a great improvement in the static as well as in the dynamic accuracy of the developed algorithms. Improved dynamic and static accuracy for the offnominal frequency deviation algorithm, and lower noise sensitivity of the small deviation algorithm are achieved by the new algorithm designs.

TEST RESULTS

The algorithms are tested using a synthesized sinusoidal signal and a voltage signal output from Electromagnetic Transient Program (EMTP) [16].

Three tests were performed using a synthesized sinusoidal signal. First, algorithm static accuracy was tested. The second test evaluated algorithm dynamic response. Third, algorithm noise sensitivity for a simulated data acquisition and signal processing system, was tested.

Transient test was performed using simulation of a fault and a load disturbance in the test system. The EMTP voltage output was used as the algorithm input signal.

Static Test

In this test, synthesized sinusoidal signals with frequencies in the range from 40 to 80 Hz in steps of 1 Hz were provided as inputs to the algorithms. Results given in Figure 1 show a comparison of the algorithm outputs. High measurement accuracy may be observed.

Dynamic Test

Frequency deviation algorithms were applied to a synthesized sinusoidal signal with an oscillating and decreasing frequency. This resembles the system frequency change in the event of power deficiency in a power system. The following equation shows the change in frequency over time:

$$f(t) = 60 - 10 \cdot t - 1 \cdot \sin(2\pi \cdot 5t) \tag{22}$$

Results in Figure 2 show a very good dynamic response of the algorithms within their range of accuracy.

Noise Test

A simple data acquisition and signal processing system is considered for the noise test. This system consists of a 12 bit analog-to-digital converter, low pass filter and one of the measurement algorithms. A sinusoidal 60 Hz signal with superimposed white zero-mean Gaussian noise was used as input for the test. The test block diagram is shown in Figure 3.

The results for the Small Deviations (SD) Algorithm and the Off-Nominal Deviations (OND) Algorithm are shown in Table 1. This table shows the relation between the mean and standard deviation of the noise and the mean and standard deviation of the relative measurement error. Since the algorithms have a very high static and dynamic accuracy within the frequency range from 54 to 66 Hz, one can assume a measurement range of 12 Hz. This range has been used for calculating the mean and standard deviation value of the relative measurement error . Results indicate that the algorithms in this system configuration do not amplify the noise and that they do not introduce a bias. They also show that the SD algorithm is slightly less influenced with noise than the OND algorithm.

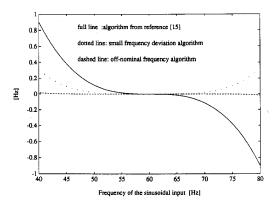


Fig. 1. Frequency Deviation Error for the Three Algorithms for the Static Test

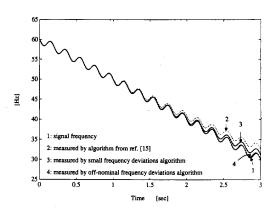


Fig. 2. Dynamic Test Results for the Three Algorithms

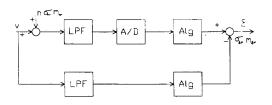


Fig. 3. Block Diagram for the Noise Test where:

v is a synthesized sinusoidal waveform.

n is a white zero mean Gaussian noise.

 σ_{nr} is the relative standard deviation of the noise.

 m_{nr} is the mean value of the noise.

 σ_{er} is the relative standard deviation of the measurement error.

 $m_{\varepsilon r}$ is the mean value of the measurement error.

LPF is Butterworth low pass filter of the fourth order with 76.8 Hz cutoff frequency.

A/D is a 12 bit analog to digital converter.

Alg is a frequency deviation algorithm.

Table 1: Noise Test Results

Meas. Number	Noise Characteristics		Output Error Characteristics	
SD alg.	m_{nri}	σ_{nri}	$m_{\epsilon ri}$	$\sigma_{\epsilon r i}$
1	-0.0059	0.0986	0.0016	0.0824
2	0.0017	0.0498	$-4.121 \cdot 10^{-4}$	0.0447
.3	$-2.06 \cdot 10^{-4}$	0.0102	-1.719-10-4	0.0111
OND alg.				
1	-0.0046	0.1033	$-1.5 \cdot 10^{-4}$	0.1129
2	$1.75 \cdot 10^{-4}$	0.0504	-1.07 ·10 ⁻⁴	0.0573
3	$-7.3 \cdot 10^{-5}$	0.099	$-2.025 \cdot 10^{-4}$	0.0119

Transient Test

Two EMTP simulations were performed. Both simulations used a model of a synchronous machine with an exciter and a governor. For the first simulation, a simple two transmission line model shown on Figure 4 was modeled. For the second simulation, system model shown on Figure 5 was used. Line Z_1 in Figure 4 and line Z_c in Figure 5 were modeled using the EMTP distributed-parameter line model. Line Z_2 in Figure 4 was modeled using the EMTP lumped-parameter line model. Node voltage output v, from the first and the second EMTP simulation, were used as inputs for the Small Deviations (SD) Algorithm and the Off-Nominal Deviations (OND) Algorithm, respectively.

For the first simulation, that used a model shown in Figure 4, a 20 milliseconds long load disturbance was applied. For the second simulation, that used a model shown in Figure 5, a three phase fault at 30 milliseconds as well as a fault clearance at 100 milliseconds were applied.

Figure 6 shows a block diagram of the measurement scheme used for testing the two algorithms.

Three tests have been performed with both algorithms. First test calculates the frequency deviation directly from the EMTP output. Second test uses a low pass filter (LPF) for filtering the EMTP output. Third test uses both LPF and the following scheme for averaging the frequency estimate:

$$\Delta \hat{f}_n^{av} = \frac{1}{8} \cdot \sum_{k=0}^{7} \Delta \hat{f}_{n-k}$$
 (23)

Test results are shown in figures 7 to 12. Figures 7 to 9 show deviation estimates calculated by the Small Deviations (SD) Algorithm. Results for the three test conditions are indicated together with the scaled change in synchronous machine velocity. Figures 10 to 12 show the same estimates for the Off-Nominal Deviations (OND) Algorithm. One can see that SD Algorithm follows the rate of change of the small frequency deviation, after filtering the input or averaging the estimate, quite accurately. The OND Algorithm follows large off-nominal deviations of frequency very accurately. In general, the transient tests performed by the authors, and not reported here, show that the SD algorithm follows more closely the small frequency deviations, whereas the OND algorithm follows more closely the large off-nominal deviations.

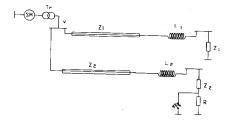


Fig. 4. EMTP System Model for Testing the Small Deviations (SD) Algorithm

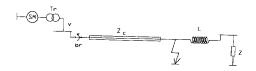


Fig. 5. EMTP System Model for Testingthe Off-Nominal Deviations (OND) Algorithm

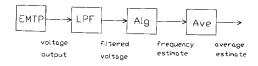


Fig. 6. Testing Scheme Using EMTP Output

LPF - Butterworth low pass filter of the fourth order

Alg - frequency deviation algorithm

AVE - eight-sample averaging unit

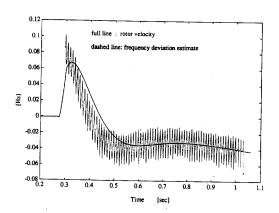


Fig. 7. SD Algorithm Estimate

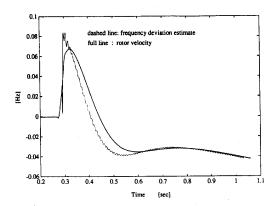


Fig. 8. SD Algorithm Estimate with Voltage Filtering

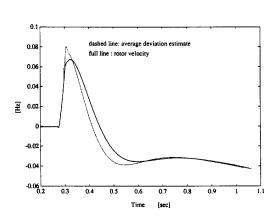


Fig. 9. SD Algorithm Average Estimate with Voltage Filtering

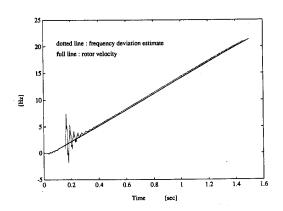


Fig. 10. OND Algorithm Estimate

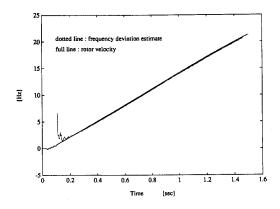


Fig. 11. OND Algorithm Estimate with Voltage Filtering

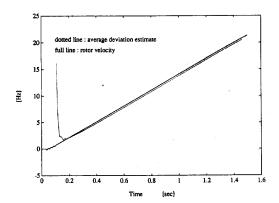


Fig. 12. OND Algorithm Average Estimate with Voltage Filtering

CONCLUSIONS

The results presented in the paper lead to the following conclusions:

- The two algorithms defined in this paper are extremely accurate and yet quite simple to implement.
- The new algorithm design approach enables definition of the generic algorithm form.
- The generic algorithm form provides a straight-forward way to define new algorithms for frequency deviation measurements.
- Algorithm implementation may be further optimized by developing a custom DSP chip that performs the calculation for a general quadratic form of signal samples.

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APPENDIX A

Quadratic forms of a signal x, denoted here as KF, may be expressed using matrix notation in the following way:

$$KF(n) = \sum_{m=0}^{N-1} \sum_{k=0}^{N-1} b_{mk} x_{n-k} x_{n-m}$$
$$= \mathbf{x}^{T} \mathbf{B} \mathbf{x}$$
(24)

where:

$$\mathbf{x}^{T} = [x_n \ x_{n-1} \dots x_{n-N+1}]$$
$$\mathbf{B} = \{b_{km}\}$$

 x_n is a signal sample at the discrete time n, **B** is the quadratic form matrix and b_{km} are the elements of this matrix.

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